

# **Exchanging Delayed Social Security Benefits for Lump Sums: Could This Incentivize Longer Work Careers?**

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October 2012

**PRC WP2012-21**  
**Pension Research Council Working Paper**  
**Pension Research Council**  
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The research reported herein was performed pursuant to a grant from the US Social Security Administration (SSA) to the Michigan Retirement Research Center (MRRC) as part of the Retirement Research Consortium. Additional research support was provided by the Deutsche Forschungsgemeinschaft (DFG), the German Investment and Asset Management Association (BVI), the Pension Research Council at The Wharton School of the University of Pennsylvania, and the Metzler Exchange Professor program. All findings, interpretations, and conclusions of this paper represent the views of the authors and not those of the Wharton School or the Pension Research Council. © 2012 Pension Research Council of the Wharton School of the University of Pennsylvania. All rights reserved.

# Exchanging Delayed Social Security Benefits for Lump Sums: Could This Incentivize Longer Work Careers?

## Abstract

Social Security benefits are currently provided as a lifelong benefit stream, though some workers would be willing to trade a portion of their annuity streams in exchange for a lump sum amount. This paper explores whether allowing people to receive a lump sum as a payment for delayed retirement rather than as an addition to their lifetime Social Security benefits might induce them to work longer. We model the factors that influence how people trade off a Social Security stream for a lump sum, and we also examine the consequences of such tradeoffs for work, retirement, and life cycle wellbeing. Our base case indicates that workers given the chance to receive their delayed retirement credit as a lump sum payment would boost their average retirement age by 1.5-2 years. This will interest policymakers seeking to reform the Social Security system without raising costs or cutting benefits, while enhancing the incentives to delay retirement.

Keywords: retirement, pension, annuity, life cycle, welfare analysis

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## **Exchanging Delayed Social Security Benefits for Lump Sums: Could This Incentivize Longer Work Careers?**

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Deciding when to retire and claim Social Security benefits is one of the most important financial decisions that people make. Traditionally, claiming triggers the beginning of a lifelong annuity payment. Yet if workers who delayed claiming were offered a lump sum instead of an actuarially-adjusted deferred annuity, it is possible that at least some would decide to work longer. This paper models the factors that influence whether individuals would be willing to trade off delayed Social Security benefits in exchange for a lump sum. Additionally, we examine the consequences of providing a lump sum reward in lieu of an actuarially-adjusted annuity for work, retirement, and life cycle wellbeing.

Economic theory suggests that retirees value lifelong income benefit streams that protect them from running out of money in old age (Yaari 1965; Davidoff et al. 2005; Mitchell et al. 1999). An implication of the theory is that most risk-averse individuals would be expected to hold a substantial portion of their portfolios in annuitized assets. Nevertheless, empirical evidence suggests that many people value lump sum payouts over lifelong benefit streams (Brown et al. 2008; Warner and Pleeter 2001). We explore these key outcomes by developing and implementing a realistically-calibrated life cycle model for forward looking rational agents with endogenous labor supply, saving, investment, and retirement decisions, that allows for time-varying investment opportunity sets and risky labor income.

The goal of this research is to evaluate whether this potential approach to Social Security reform would induce workers to retire later on a voluntary basis. We find that such a policy has the potential to increase retirement ages substantially, with little or no decline in welfare. Three factors help explain why the lump sum reward for deferred retirement can induce more work while not decreasing lifetime utility. First, many people would prefer to

have a lump sum rather than an addition to their lifetime Social Security benefit, as this affords them flexibility over the timing of their consumption and leisure decisions. A second reason is liquidity driven: that is, if people desire to leave a stock of assets to their heirs, having a lump sum enhances this possibility. And third, financially sophisticated individuals able to participate in the equity market will find attractive the opportunity to invest some of their lump sum amounts.

Policymakers seeking ways to reform the Social Security system may be interested in our findings, since the actuarially fair lump sum for delayed retirement does induce some individuals to work longer voluntarily. In our base case, workers given the chance to receive their delayed retirement credit as a lump sum payment would boost their average retirement age by 1.5-2 years. Moreover, when the reform is implemented, this boosts the probability of working beyond the normal retirement age from 29% to 86% for the young, and from 4% to 49% for 60-year olds. Results vary, of course, across individuals of different types: the effect is even larger for less risk-averse older households, while the most risk-averse respond least. Financially unsophisticated households (i.e. those who lack access to the equity market) are also relatively unresponsive to the lump sum option; even here, though, the less risk-averse still tend to work longer and retire later. Moreover, we show that such a lump sum policy would generally not detract from wellbeing: in the base case, young workers typically have virtually no change in lifetime utility, whereas older individuals gain slightly. Among the less financially sophisticated, both the young and the old experience little change.

It is worth noting that offering a lump sum equivalent in expected present value to the delayed retirement credit would be cost-neutral to the system, on average. Additionally, if older individuals worked longer voluntarily, this could enhance system solvency via additional payroll tax collections.

## Prior Studies

This paper contributes to the research examining the effects of Social Security policies on labor supply.<sup>1</sup> A number of studies in the portfolio choice literature have investigated how individuals might alter their work, investment, annuitization, and retirement decisions in response to change in Social Security benefits assuming a parameterization similar to that in the US Social Security system.<sup>2</sup> Yet these analyses have not examined optimal household life cycle behavior with flexible work hours and retirement, to assess what might happen if people were afforded the opportunity to take part of their Social Security benefits as a lump sum instead of as a benefit flow.

Experimental research and survey evidence has suggested that a majority of workers would favor lump-sum payments over lifetime benefits, if these were approximately actuarially equivalent. Furthermore, there is some modest price sensitivity associated with this preference (Brown et al. 2008, 2011). Orszag (2001) discussed some important institutional design aspects of Social Security (e.g. computation of present values, spousal/widow benefits) and offered comments on how lump sum benefits might replace the delayed retirement (annuity) credit. His work provided some preliminary evidence that claiming probabilities could rise in response. Fetherstonhaugh and Ross (1999) reported that for 80 percent of their survey respondents, a lump-sum payment instead of an increase in annual benefit amounts due to delayed claiming would provide an incentive to claim later. Nevertheless, those studies focus specifically on the claiming decision (and how these decisions are framed), but they abstract from other important factors including preferences (risk aversion, leisure, impatience), the state of the business cycle, uncertainty with respect to labor income and capital markets, asset allocation, household saving, and health status. Most importantly, they assume that the claiming decision is independent of labor force participation. Therefore that

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<sup>1</sup> See Feldstein and Leibman (2002) for a review, and most recently, Laitner and Silverman (2012).

<sup>2</sup> See Kotlikoff, and Viceira (2008), Chai, Horneff, Maurer, and Mitchell (2011) and Chai, Maurer, Mitchell, and Rogalla (2012).

research is silent on the likely impact of such lump-sum options on work hours, retirement ages, saving, and household wellbeing. Moreover, offering such lump-sums could potentially induce workers to delay retirement and claiming of Social Security benefits, which could enhance system sustainability. There has been no theoretical research on this topic to date.

## Methodology

Our prior work on which we build this study developed, implemented, and calibrated a realistic discrete time life cycle model of endogenous work hours, retirement behavior, consumption, saving, and portfolio choice (c.f. Chai, Maurer, Mitchell, and Rogalla 2012). Allowing for uninsurable labor income risk and capital market risk, this model incorporates individual risk aversion, time preferences, and leisure preferences, as well as borrowing constraint, and uncertain length of life. Preferences in each period are characterized by an iso-elastic and time-separable power utility function defined over a composite good consisting of consumption  $C_t$  and leisure  $L_t$  at time  $t$ , and wealth  $Q_t$  bequeathed to the next generation.

As is conventional in the theoretical literature, the relative importance of leisure and consumption is valued using a modified Cobb-Douglas function, which ensures that the elasticity of substitution between consumption and leisure is equal to one. The value function is given by:

$$V_t = \frac{(C_t L_t^\alpha)^{1-\rho}}{1-\rho} + \beta E_t \left( p_t V_{t+1} + (1-p_t) b \frac{(Q_{t+1})^{1-\rho}}{1-\rho} \right) \quad (1)$$

with terminal utility (at age 100)  $V_T = \frac{(C_T L_T^\alpha)^{1-\rho}}{1-\rho} + \beta E_T \left( b \frac{(Q_{T+1})^{1-\rho}}{1-\rho} \right)$ . The parameter  $p_t$  denotes the subjective probability of surviving to time  $t + 1$ , given the consumer is alive at  $t$ . The parameter  $\rho$  is the coefficient of relative risk aversion, and  $\beta$  is the rate of time preference. Leisure preferences are governed by the parameter  $\alpha$ . The strength of the bequest motive is controlled by the parameter  $b$ . In each period, the individual must decide how much to work,

consume, and invest in the capital market. Also the worker must decide when to retire and claim Social Security benefits. This problem is solved through backward induction of the value function. The optimal policies are then evaluated by conducting a Monte Carlo simulation (for further details see Appendix A). For the base case worker, preference parameters are set as follows: coefficient of relative risk aversion  $\rho = 5$ , discount factor  $\beta = 0.97$ , leisure preference value  $\alpha = 1.3$ , and bequest strength  $b = 0$ . The one-period survival rates  $p_t$  are taken from the US 2000 population mortality table for females.<sup>3</sup> In additional sensitivity analysis we vary preference parameters.

The stock and labor market processes are governed by a “regime-switching” process for the business cycle. Asset returns are characterized by either a ‘normal’ capital market (with low volatility/high expected returns) or a ‘crisis’ scenario (with high volatility/low expected returns). The deterministic component of the wage rate process and the labor income shock process follows Chai, Maurer, Mitchell, and Rogalla (2012). Housing-related expenditures are estimated using data from the Consumer Expenditure Survey (as described in Appendix B).

We also implement a realistic approach to determining Social Security benefits, where the worker may claim a benefit between the early retirement age (*ERA*) of 62 and the late retirement age (*LRA*) of 70. If the worker claims prior to her normal retirement age (*NRA*), she receives a permanently lower benefit for life; if she claims later, her Social Security benefit payment is increased by the delayed retirement credit. For our alternative scenario, we examine how retirement behavior would change if the individual could take a part of her Social Security benefits as a lump sum payment, by working beyond the *NRA*. This lump sum payment would be equal, in present value terms, to the additional benefit stream paid to the worker claiming Social Security benefits after the *NRA*.

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<sup>3</sup> Using a similar model framework; Chai, Horneff, Maurer, and Mitchell (2011) show that these parameter values replicate several empirical facts including the hump-shaped pattern of work hours, the two peaks in retirement rates, and the sizeable decline in consumption at retirement.

Several factors might be anticipated to lead people to favor a lump sum over an annuity stream. For instance, people might wish to leave a bequest, have a higher or lower discount rate, value leisure strongly, or be very risk-averse. Other influences could include changes in the retirement system such as a lower replacement rate and a higher normal retirement age. We also explore how financial sophistication might shape peoples' responses to the Social Security lump sum option versus the annuity. This takes into account the finding that many Americans lack knowledge of and easy access to sophisticated financial instruments such as equities (Lusardi and Mitchell 2007; Gomes and Michaelides 2005).<sup>4</sup> Additionally we provide a welfare analysis which evaluates the extent to which the ability to convert deferred Social Security benefits into a lump sum can enhance worker wellbeing.

In what follows, we present results for individuals initially observed at age 20, and separately at age 60. This allows us to explore the likely behavioral responses of older versus younger workers. We present two sets of results: in the base case, workers have access to the stock and the bond market, which we deem the financially sophisticated group. In an alternative scenario, the analysis assumes that individuals can hold only bonds paying a safe return, but they have no access to equities. The model assumes that 20-year olds hold no initial wealth. For 60-year olds, we estimate distributions of income and wealth-to-income ratios using the Health and Retirement Study (HRS) for single female households.<sup>5</sup> To this end, we first group all households initially aged 60 into two categories: stockholders and non-stockholders. Then, within each household category, we drop the lower and upper labor income quartiles (to avoid data outliers). Hence, there are 50 labor income percentiles left (i.e. the 25<sup>th</sup> -74<sup>th</sup> percentile).<sup>6</sup> In order to specify distinct combinations of wealth-to-income ratios

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<sup>4</sup> Using a dataset on Swedish investors, Calvet, Campbell, and Sodini (2009) find empirical evidence that the share of risky assets held by households is strongly positively correlated with an index for financial sophistication.

<sup>5</sup> The HRS (here we use waves one to ten) is a longitudinal panel study which surveys a representative sample of over 26,000 respondents age 50+ every two years; see <http://hrsonline.isr.umich.edu/>.

<sup>6</sup> This procedure generates wealth-to-income-ratios for stockholders (non-stockholders) with a mean value of 3.76 (1.31), and a standard-deviation of 1.7 (0.75).

and labor income percentiles, we estimate average wealth-to-income ratios for each of the 50 income percentiles. We then simulate 10,000 life cycle paths for every combination of wealth-to-income ratios and income quantiles using optimal feedback controls obtained from the numerical optimization model. All results are reported as the average of 50,000 paths (i.e.  $50 \times 10,000$ ).

## Results

Under the Social Security system's current rules, a worker who delays claiming her benefit until after the Normal Retirement Age (NRA) is entitled to a benefit increase of about 8% per year that retirement is deferred.<sup>7</sup> In our model, under an actuarially fair lump sum scheme, an individual who opted to work to age 66 instead of claiming benefits at age 65 would then receive a lump sum worth of about 1.2 times her age-65 benefit, plus the age-65 benefit stream for life. Similarly, an individual deferring retirement even later, to age 70, would receive a lump sum worth about 6 times the starting-age annual benefit payment, plus the age-65 benefit stream for life (see Appendix A for details).

### *Results for the Base Case*

To illustrate how our life cycle model works, we refer to the base case results in Figure 1. Average consumption increases with age in the top panel, since workers are not able to borrow against future labor income. Consistent with empirical evidence,<sup>8</sup> consumption drops sharply around the retirement age and continues to decrease thereafter. The model also generates a relatively realistic work hours profile by age, as reported in the second panel.

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<sup>7</sup> The Social Security delayed retirement credit of 8% per year's delay was intended to be actuarially fair at the time the law was passed; this was consistent with average mortality tables at the time, as well as a 2.9% real assumed interest rate. In this paper we assume a real interest rate of 2%, a rate more consistent with the current low interest rate regime. As Shoven and Slavov (2012) note, in such a case the delayed retirement credit of 8% per annum will be better than actuarially fair for most people, thus embodying additional incentives to defer retirement. To the extent this is true, the lump sums we compute are also better than actuarially fair with respect to the 2.9% assumption.

<sup>8</sup> See Bernheim, Skinner and Weinberg (2001), Banks, Blundell, and Tanner (1998), Battistin, Brugiavini, and Weber (2009), and the discussion in Chai, Horneff, Maurer, and Mitchell (2011).

Younger workers in their 20's and 30's work more than 40 hours per week. Individuals in their 40's (50's) devote about 40 (35) hours per week to their jobs; after that, they sharply cut back on average work hours and start to retire from full-time employment.<sup>9</sup> The third panel reports asset allocation patterns by age. For those age 20-30, the bond fraction is 60%, somewhat higher than found in empirical work. Yet from their 30's onward, individuals hold about 30-40% of their wealth in bonds, and 60-70% in stocks; these ratios are in line with empirical evidence.<sup>10</sup> Overall, our life cycle model is able to generate consumption, work, and investment patterns that accord reasonably well with empirical evidence.

*Figure 1 here*

Next we examine how the two different delayed retirement schemes affect results in the base case for individuals initially age 20 (left side of Figure 1) versus age 60 (right side). Offering a lump sum Social Security instead of a larger benefit payment for deferred retirement changes life cycle consumption, work hours, and investment patterns. For the younger group, consumption and work hours do not respond much until they reach their 60's. At that point, those who will receive the lump sum can consume more and enjoy less leisure. This occurs because the lump sum can be spent as well as invested, potentially earning a market return that permits more spending. Additionally, this higher consumption is traded off for less leisure at older ages (more work hours). Overall, asset allocation under the two scenarios is also quite similar, though after age 60, having the lump sum leads to a slightly higher equity exposure and hence slightly lower bond fraction. Similarly, for those age 60 when the lump sum is introduced, consumption and work hours increase, while bond holdings fall slightly.

Additional detail on retirement patterns is provided in Table 1, where young people – knowing they will receive a lump sum for deferred retirement – shift rather markedly toward later retirement. In fact, the left panel indicates that the average retirement age rises by 1.8

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<sup>9</sup> For more on this point see Chai, Horneff, Maurer, and Mitchell (2011).

<sup>10</sup> See for example Gomes and Michaelides (2005).

years (from 64.5 to 66.3); the probability of claiming benefits after the NRA rises from 29% to 86%. Among those already age 60 when the lump sum scenario is implemented (right panel), the average retirement age again rises though by a bit less, 1.4 years (from 63.5 to 64.9). While most older workers do claim benefits by age 68, their probability of working beyond the NRA rises substantially, from 4% to 49%.<sup>11</sup>

*Table 1 here*

#### *Sensitivity Analysis*

Thus far, results for the base case provide support for the conclusion that providing a lump sum instead of an increased annuity benefit for deferred retirement under Social Security would induce people to work longer. Next, in sensitivity analyses presented in Table 2, we explore what happens when key preference parameters are changed. In addition, we analyze the impact of two other potential changes in the Social Security rules, reported in Panel A. Finally, Panel B illustrates the policy impacts on households who do not access the equity market.

*Table 2 here*

Several alternative calibrations for preference parameters are provided in Table 2, to be compared with the average retirement age results for the base case as well as the estimated probability of working beyond the normal retirement age. Interestingly, workers with a moderate versus a strong bequest motive ( $b = 2$  or  $5$  in Panel A), compared to the base case without bequests, behave relatively similarly when given a lump sum instead of a delayed retirement annuity. Thus young workers seeking to leave a bequest would defer retirement by 1.9 years, on average, versus 1.8 if they had no interest in bequests; the older group would boost its retirement age by 1.3 years versus 1.4 with no bequest motive. It is also worth noting

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<sup>11</sup> Table 1 shows two spikes in retirement frequency, at ages 63 and 66 (for the group initially age 20). These are slightly later than the two retirement peaks at age 62 and 65 reported by Gustman and Steinmeier (2005). Yet that study denotes people as retired if they leave full-time work, while we assume that individuals claim retirement benefits and move to full leisure at the same age. If we define retirement as working less than 20 hours per week, this would shift retirement rates earlier.

that the probabilities of working beyond the NRA are comparable across the board. In sum, even when workers have a bequest motive, the delayed retirement impact of the reform is similar. Accordingly, providing a lump sum does not simply result in wealth transfers to one's heirs, consistent with the rationale for Social Security as a national social insurance scheme intended to support consumption for the elderly.

The next six rows of Panel A in Table 2 illustrate how results change for lower/higher subjective discount rates, lower/higher risk aversion, and lower/higher levels of tastes for leisure versus consumption. Less patient younger and older workers ( $\beta = 0.96$ ) will choose to retire earlier as compared to the base case, but the lump sum reform still induces more to work beyond the normal retirement age, and on average retirement ages rise. As discount rates fall, those who are more patient ( $\beta = 0.99$ ) will work longer than in the base case, with an average increase of over one year in the retirement age; here too, the lump sum induces later retirement. Turning next to differences by level of risk tolerance, older workers who are not particularly risk averse ( $\rho = 2$ ) will retire at the same age as in the base case. Yet offering them the lump sum instead of the delayed annuity credit produces a much larger impact on retirement ages: on average, the retirement age rises by 3.3 years compared to 1.3 in the base case. A young household with low risk aversion retires 1.8 years earlier on average than the base case household but delays retirement by a comparable 1.6 years in the lump sum regime. Early retirement is also the norm for the extraordinarily risk averse ( $\rho = 8$ ), under any of the circumstances depicted. This is because such individuals tend to work very hard and save a great deal at younger ages to protect against shocks; then, as they approach their 60's, they favor certain leisure and early retirement instead of worrying about not being able to consume due to uncertain mortality. Additionally, offering them a lump sum has hardly any effect on retirement behavior.

Next we turn to two alternative formulations for leisure preferences: one individual

values consumption much more highly ( $\alpha = 0.7$ ) than in the base case, and the other values leisure more ( $\alpha = 1.9$ ). Here, the lump sum reform has virtually no impact. That is, leisure lovers still quit work early, and those who strongly prefer consumption still retire later since longer worklives generate more spendable income.

The final two rows of Panel A in Table 2 examine the impact of two variations on Social Security system parameters. Not surprisingly, if the Social Security benefit replacement rate were reduced from  $\lambda = 60\%$  to 45%, retirement ages rise substantially. Those who have a lifetime to adjust, who are initially age 20, work 2.7 years longer, and the older group works 3.3 more years. In both instances the probability of working over the NRA exceeds 90%. This result obtains regardless of whether the delayed retirement credit is replaced by the lump sum. In our second policy variant, we raise the NRA from 65 to 67 for those initially age 20. This again would raise the average retirement age in the annuity regime, but moving to the lump sum scenario would have hardly any additional impact on retirement behavior.

If the aim is to raise retirement ages, the last two policies work in the same direction as replacing the delayed retirement credit with a lump sum as described above. Yet cutting the replacement rate and raising the NRA will be politically unpopular, since these represent benefit reductions; offering the lump sum does not represent a benefit cut but a rather a change in the timing of benefit receipt.

To this point, we have assumed that consumers have access to the equity market if they wish to allocate their portfolios across risky and risk-free assets. Panel B illustrates results if consumers do not access the equity market. This might be the case for people who are not financially savvy due to lack of time, information, or the requisite guidance on how to buy stock. We call this group the financially unsophisticated, consistent with van Rooij, Lusardi and Alessie (2011) who show that those who lack financial literacy do not invest in

the stock market. It is well known that some 50% of households do not participate in the stock market today (SCF, 2012; Gomes and Michaelides, 2005); hence for this group, this second set of results could be relevant.

Once again, we evaluate how retirement ages would change if the lump sum were offered in lieu of the Social Security delayed benefit. The first row indicates that, in the base case, both the young and the old would retire later than in Panel A. But giving workers a lump sum for deferred retirement instead of an increased annuity would be less effective in inducing prolonged work at older ages.

The second row of Panel B indicates that people who love risk ( $\rho = 2$ ) worry less about smoothing consumption, so for them the lump sum induces longer work and higher consumption. By contrast, for extremely risk averse younger individuals ( $\rho = 8$ ), the reform has again the opposite incentive: they retire earlier and have a much lower probability of working beyond the Normal Retirement Age. This can be explained by the fact that the financially unsophisticated place a high value on the Social Security annuity as it allows them to smooth consumption and also protects against longevity risk. These individuals cannot replicate the benefit stream by investing the lump sum in the bond market. Evidently, boosting Americans' level of financial literacy would help strengthen the incentive effects of a lump sum reform.

### **Welfare Implications**

Finally we turn to an analysis of the welfare implications of replacing the delayed retirement benefit with a lump sum. The approach evaluates how much additional wealth (as a percent of first-year labor earnings) the individual would need under the current regime, to be as well off as under the lump sum regime. Accordingly, a positive value implies the reform is welfare enhancing, while a negative value implies the opposite.

Table 3 reports the results for various parameterizations of people initially age 20 and

age 60 when the reform is implemented. In the base case, the change in welfare for the young is miniscule (10 basis points). For those age 60 when the reform is implemented, the change in lifetime utility is valued slightly positively, at 4%. Under alternative preference settings, there is virtually no impact on the young – the welfare changes in all cases do not exceed -1%. Moreover, the young financially unsophisticated also experience almost no change in utility, with the exception of the very risk averse, where lifetime welfare declines by 10% of the initial labor income.

*Table 3 here*

Turning to the older group (initially age 60), welfare impacts are all positive but relatively small (below 5%) in most cases. One exception is for the risk-lover ( $\rho = 2$ ) who has access to the stock market. Here, the consumer's welfare gains amount to a substantial 29%, because she can trade off higher consumption levels early in retirement in exchange for lower consumption later (when mortality risk increases). Moreover she has access to the equity market and can invest part (or all) of the lump sum. The welfare gain is much lower (18%) when the worker does not invest in the equity market.

For two groups of older individuals, welfare rises under the lump sum regime, but there is little impact on retirement (see Table 2). Those with little taste for leisure ( $\alpha = 0.7$ ) appreciate the lump sum but do not change work patterns as compared to the annuity regime; this is because they are already willing to work a long time (up to age 70, in some cases) to finance their high consumption needs. Their lengthy worklives generate high lump sum payments for the delayed retirement credit, which in turn can be invested in the stock market and used to boost consumption. The welfare gains of a lump sum payment compared to higher annuity benefits disappears for 60-year old work lovers ( $\alpha = 0.7$ ) with no access to the stock market.<sup>12</sup>

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<sup>12</sup> Such preferences for very long worklife may not be relevant for the broader population, but they would apply to tenured university professors (Ashenfelter and Card, 2002).

The retiree with a less generous replacement ratio ( $\lambda = 0.45$ ) profits by receiving the delayed retirement credit as a lump sum instead of a higher lifelong pension (welfare rises by 22.3%). Again, the reform has little impact on work effort, because in both cases the retiree is willing to work longer to compensate the lower replacement rate. Rather the welfare improvement results again from the possibility to invest the lump sum in the stock market.<sup>13</sup>

In general, the lump sum reform offers an incentive for people to trade off more consumption for less leisure, by working longer and deferring retirement. Overall, this reform has little impact on the young, relatively speaking, and it slightly enhances welfare among the older population. Accordingly, such a reform could be an appealing alternative to encourage longer worklives.

## Conclusions

This paper has explored whether people might voluntarily work longer if they were offered a lump sum instead of a delayed retirement annuity under Social Security. We adopt a realistically calibrated life cycle model with forward looking rational agents with endogenous labor supply, saving, investment, and retirement decisions, and allowing for time-varying investment opportunity sets and risky labor income. This model generates consumption, work, and investment profiles, relatively consistent with empirical evidence.

We show theoretically that substituting a lump sum for the delayed Social Security annuity provides an incentive for many workers to voluntarily defer retirement, with little reduction in lifetime welfare. In other words, giving workers a lump sum at their delayed retirement date permits them to adjust the timing of their consumption and leisure time to adapt their preferences. People who receive their delayed retirement credit as a lump sum payment should optimally boost their average retirement age by 1.5-2 years. Having a lump sum in lieu of a higher lifetime Social Security benefit allows retirees to shift consumption to

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<sup>13</sup> For consumers lacking access to the stock market, the welfare gain is positive but small (less than 2%).

the earlier phase of retirement when mortality risk is low. In addition, the lump sum payment permits households to participate in the stock market, seeking to earn the risk premium. These results hold whether or not workers have a positive bequest motive, implying that the lump sum does not simply result in wealth transfers to theirs. Households without access to the equity market are less responsive to the lump sum option, but even here, the less risk-averse also work longer and retire later, and the lump sum policy generally does not detract from wellbeing.

In years to come, US policymakers will be actively seeking ways to reform Social Security to restore the system to solvency. Proposing cuts in benefits tends to be quite politically difficult. By contrast, offering a fair lump sum in place of the delayed retirement annuity credit may be more politically attractive. By (voluntarily) delaying their retirement date due to the lump sum option, workers would continue to pay Social Security payroll taxes for more years, which could help return the system to solvency via additional payroll tax collections. Moreover, such a policy could be designed to be cost-neutral, albeit in the real world one would also need to consider additional issues including spouse and survivor benefits, changes in annuity factors, sudden demands for liquidity due to health shocks, and other factors. These are all avenues of future research.

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## Appendix A: The Life Cycle Model

We build on the framework developed and calibrated by Chai, Maurer, Mitchell, and Rogalla (2012). Stock returns and labor earnings are driven by a Markov-Regime-Switching process for the business cycle with two states: normal ( $s_t = 0$ ), or contraction ( $s_t = 1$ ). The consumer observes the current state and knows the (constant) conditional transition probabilities  $\pi_{i,j}^{BC} := P(s_{t+1} = j | s_t = i)$  to be at time  $t+1$  in state  $j$ , given that at time  $t$  the economy is in state  $i$ . Using US Gross National Product data, we estimate the transition probabilities between the two states as  $\pi_{0,0}^{BC} = \pi_{0,0}^{BC} = 0.68$  and  $\pi_{0,1}^{BC} = \pi_{0,1}^{BC} = 0.32$ .<sup>14</sup> Capital markets include riskless bonds with gross return  $R_f = 1.02$  and risky stocks. Log stock returns  $\ln(R_{s,t+1}) \sim N(\mu_i, \sigma_i)$  are normally distributed with state dependent parameters by either being in a normal capital market regime with low volatility ( $\sigma_0 = 11.21$  percent) and high expected returns ( $\mu_0 = 6.84$  percent), or a contraction regime with high volatility ( $\sigma_1 = 20.77$  percent) and low expected returns ( $\mu_1 = 2.12$  percent). Income on assets is taxed according to the proportional rate  $\theta^c$ , which we set to 20 percent.

The labor income process allows for unemployment risk and state-dependent wage rate dynamics. The individual receives uncertain labor income depending on what fraction of available time is devoted to work ( $1 - L_t$ ) and a state dependent wage rate  $WR_{s,t+1}$ . Earnings from the labor market are reduced by an age-dependent fraction  $q_{t+1}$  of housing related expenditures, estimated using data from the Consumer Expenditure Survey (or CES) as shown in Appendix B. In addition, the worker must pay income taxes according to a proportional tax rate  $\theta^l$  equal to 30 percent. Thus disposable yearly labor earnings before the (endogenous) retirement age ( $t < \tau$ ,  $\tau \in [62, 63, \dots, 70]$ ) are given by:

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<sup>14</sup> As in Storesletten, Telmer, and Yaron (2004) a contraction (expansion) state occurs when the GNP growth rate was less than (greater than) its sample period mean.

$$Y_{s,t+1}^E = (1 - q_{t+1}) \cdot (1 - \theta^t) \cdot WR_{s,t+1} \cdot (1 - L_t) \quad (\text{A-1})$$

Here  $L_t = [1/3, 1]$  stands for leisure and is measured as a percentage of available time. To transfer normalized leisure into work hours we assume 100 waking hours per week. The exogenously- determined wage rate process is given by  $WR_{s,t+1} = \exp(w_{t+1}) \cdot E_{s,t+1} \cdot U_{t+1}$ . The deterministic trend component  $w_{t+1}$  is calibrated using the earnings function reported in Fehr, Jokisch, and Kotlikoff (2006) for middle-income workers,<sup>15</sup> and it is scaled to generate an average gross labor income of \$20,000 at age 20.  $\ln(U_{t+1}) \sim N(0, \sigma_u)$  is a state-independent transitory shock ( $\sigma_u = 32.9$  percent),<sup>16</sup> and  $E_{s,t+1} = E_{s,t} n_{s,t+1}$  is a state-dependent permanent labor earnings component, with  $\ln(n_{s,t+1}) \sim N(0, \sigma_{n,s})$ . We follow Storesletten, Telmer, and Yaron (2004) and set the state dependent volatility  $\sigma_{n,s}$  of permanent wage rates shocks in the normal state to  $\sigma_{n,0} = 8.4$  percent which is lower than in the contraction scenario  $\sigma_{n,1} = 15.9$  percent. The correlation between stock returns and permanent and transitory earnings shocks  $\phi$  for both cases is set to 0.2.

The worker could be unemployed in the next period, where the state-dependent probability of unemployment  $\pi_s^U$  is again lower in the normal state ( $\pi_0^U = 5$  percent) than in the contraction state ( $\pi_1^U = 10$  percent). In such a situation, the worker receives unemployment compensation at time  $t + 1$  specified as a set fraction of labor income, i.e.,  $Y_{s,t+1}^U = 0.6 \cdot Y_{s,t+1}^E$ .

The model allows a flexible retirement age, i.e. the worker can claim a Social Security benefit payable for life at any age between the early retirement age ( $ERA = 62$ ) and the latest retirement age ( $LRA = 70$ ). Once benefits are claimed, the individual does not return to the workforce. If the worker claims prior to the normal retirement age ( $NRA = 65$ ), the benefits are

<sup>15</sup> Precisely we use equation (9) with parameter  $\lambda=0$  which produces a humped shaped trend function for wages rates:  $w(\text{age}) = \exp(4.47 + 0.033 \cdot \text{age} - 0.00067 \cdot \text{age}^2)$ .

<sup>16</sup> The volatility of the transitory shock is estimated by averaging the fixed effect and measurement error from Storesletten, Telmer, and Yaron (2004).

permanently reduced for each year of early retirement according to the reduction factor  $g_1 = 0.0713$ . If the individual works longer than the NRA, the Social Security benefit is increased per year of additional work by the delayed retirement credit  $g_2 = 0.077$  (see Buchinsky, Rust, and Benitez-Silva 2000). To capture this feature, we calculate the after-tax Social Security benefits as in Chai, Horneff, Maurer, and Mitchell (2011):

$$Y_t = (1 - q_t)(1 - \theta^r) \bar{Y} \lambda F_{\tau, NRA}, \quad (\text{A-2})$$

where  $F_{\tau, NRA} = \exp(-g_1(NRA - \tau)) \cdot I_{\{\tau \leq NRA\}} + \exp(-g_2(NRA - \tau)) \cdot I_{\{\tau > NRA\}}$  a factor which specifies the reduction/increase of retirement benefits if the individual retires prior/after to the NRA. The parameter  $\lambda$  is the Social Security replacement rate (here set to 60 percent as in Mitchell and Phillips 2006) based on the worker's lifetime average earnings approximated by  $\bar{Y} = (\sum_{t=1}^K (1 - \bar{L}) \exp(w(t))/K) \cdot E_K$ . Here  $K$  denotes when the individual attains the normal retirement age ( $NRA$ ) and  $1 - \bar{L}$  stands for the average working time until retirement, which we set equal to 0.4 corresponding to a lifetime work effort of 40 hours per week on average. As in Gomes, Kotlikoff, and Viceira (2008) Social Security benefits are taxed at a proportional rate of  $\theta^r = 15$  percent.

Alternatively, we posit that the individual can receive the delayed Social Security retirement benefit as a lump sum payment, instead of an increase in lifelong annuity benefits. In this case, the lump sum payment is calculated as the actuarial present value of the additional annuity benefits generated by working longer than the normal retirement age. Formally the lump sum payment is given ( $t > NRA$ ) as follows:

$$LS_t = (1 - \theta^r) \cdot \bar{Y} \lambda (F_{\tau, NRA} - 1) \cdot \ddot{a}_t \quad (\text{A-3})$$

Here  $\ddot{a}_t = 1 + \sum_{m=1}^{T-1} (\prod_{u=t}^{t+m-1} p_u) \cdot R_f^{-m}$  is the actuarial present value factor based on the riskless interest rate  $R_f$  and the one year survival probabilities  $p_t$  (i.e. to survive to time  $t+1$  given being alive at  $t$ ).

The following table illustrates the possible lump sum payments for delaying retirement as percentage of benefits at age 65 (*ceteribus paribus*). To calculate them, we use a riskless interest rate of 2% per annum (as in our life cycle model) and the US 2000 population mortality table for females. Further we normalize the lump sum payments given in equation (A-3) by  $(1 - \theta^r) \bar{Y} \lambda$ . In addition we report the delayed retirement credits  $F_{\tau, NRA}$  if the worker receives the additional benefits as a lifelong annuity.

	Retirement Age				
	66	67	68	69	70
Life Annuity (in % of NRA benefit)	8.0	16.6	26.0	36.1	46.9
Lump Sum (in % of NRA benefit)	119.0	239.2	360.0	481.1	602.9

Each period, the consumer decides how much to work  $(1 - L_t)$  to generate labor income, when to retire, and how to allocate cash on hand  $W_t$  to bonds  $B_t$ , stocks  $S_t$ , and consumption  $C_t$ . The budget constraint is given by:

$$W_t = S_t + B_t + C_t, \quad (\text{A-4})$$

and next period's wealth  $W_{t+1}$  is described by:

$$W_{t+1} = (S_t R_{s,t+1} + B_t R_f)(1 - \theta^c) + \theta^c (B_t + S_t) + Y_{s,t+1} \quad (\text{A-5})$$

Here,  $Y_{s,t}$  is labor income as defined in equations (A-1) and (A-2). This is the state-dependent net labor income (or unemployment benefits) prior to claiming and the Social Security benefits after claiming. In case the household claims after the NRA, the delayed retirement credit is paid in form of a lump sum, and  $g_2$  in equation (A-2) is set to zero when calculating the lifelong benefits from Social Security. In this situation, the wealth transition equation at the time of claiming,  $\bar{t}$ , is given by:

$$W_{t+1} = (S_t R_{s,t+1} + B_t R_f)(1 - \theta^c) + \theta^c (B_t + S_t) + Y_{s,t+1} + LS_{t+1} \quad (\text{A-6})$$

Here  $LS_t$  is the lump sum payment according to equation (A-3) the household receives at time  $\bar{t} + 1$ . In subsequent periods ( $t > \bar{t}$ ), the transition equation is again given by (A-5).

Households cannot borrow against human capital nor can they hold short positions in stocks and bonds ( $C_t, S_t, B_t \geq 0$ ). Moreover, we posit that in order to participate in the stock market, the household has to be willing and able to invest a minimum amount in stocks (as in Smetters and Chen, 2010). This amount is set to 50% of permanent labor income.

The individual's optimization problem is now to maximize lifetime utility with respect to her asset allocation between bonds and stocks, consumption, work hours, and the retirement decision. After normalizing with permanent labor income there are four state variables: cash on hand  $W_t$ , retirement age  $\tau$ , the business cycle state  $s$ , and age  $t$ . We discretize the (normalized) continuous state variable and solve the optimization problem by backward induction. For computations, we use a grid of dimension  $40(W) \times 2(s) \times 42(t)$  before and  $40(W) \times 2(s) \times 39(t) \times 9(\tau)$  after the *ERA*. For each grid point we evaluate the policy and value functions using Gaussian quadrature integration and cubic-splines interpolation.

## **Appendix B.** *Construction of Housing-related Expenditure to Income Ratios*

The Consumer Expenditure Survey (or CES) is collected by the U.S. Federal government through the Bureau of Labor Statistics, for the purpose of providing a complete range of information on consumer expenditures and income. The survey consists of five interviews on a quarterly basis. At the initial interview, each household must complete a consumption diary over a 2-week span and provide a detailed overview of what it consumes on a daily basis. The subsequent four interviews focus on quarterly expenditures and annual income; expenditures on housing in the current quarter we multiply by four to obtain annual housing expenditures. Our dataset spans the time period 1996 to 2010 and represents a panel over one-period horizons, but different households are interviewed on a year-to-year basis. In total, there were 425,672 interviews of 145,203 unique households over the 15-year period. We consider only households where the head is between ages 20-89; we omit observations with negative housing expenditures or labor income. In addition, any observation with a housing-expenditure-to-labor-income ratio exceeding one is excluded from the analysis. This leaves 116,015 households and 161,050 yearly observations.

The variables of interest relate to housing expenditures and labor income to generate a ratio of ‘Housing Expenditure over Labor Income.’ We sought to fit this measure as closely as possible to the specification reported in Gomes and Michaelides (2005). We define annual labor income as  $\text{FINCBTAX} - (\text{INTEARNX} + \text{FININCX})$ , described as ‘Income before taxes’ less ‘income from savings and bonds’ and ‘income from dividends, royalties, etc.’<sup>17</sup> Quarterly housing expenditures are estimated as the sum of the variables  $\text{HOUSCQ}$  and  $\text{HOUSPQ}$ , and this we multiply by four to obtain annual housing expenditures. The last pertinent variable for analysis is the age of the reference person, which is  $\text{AGE}$ .

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<sup>17</sup> One might ask why we do not use the income after taxes ( $\text{FINCATAX}$ ). We discovered that, for some households reporting an income of zero ( $\text{FINCBTAX}=0$ ), they still had to pay some taxes so the after-tax income was negative. This poses a problem for computing the ratio of Housing Expenditures to Labor Income.

Next we run a regression of the ratio of housing expenditures to labor income ( $q_{i,t}$ ) on age polynomials and an economy dummy. The ratios are computed for each household by taking housing expenditures (mortgage/rent payments, utilities, and housing-related durable expenditures) relative to the before-tax labor income and regressed against a cubic polynomial of age (of the head of the household), and a dummy variable representing an economy that is either normal (=0) or contracting (=1). The regression is as follows:

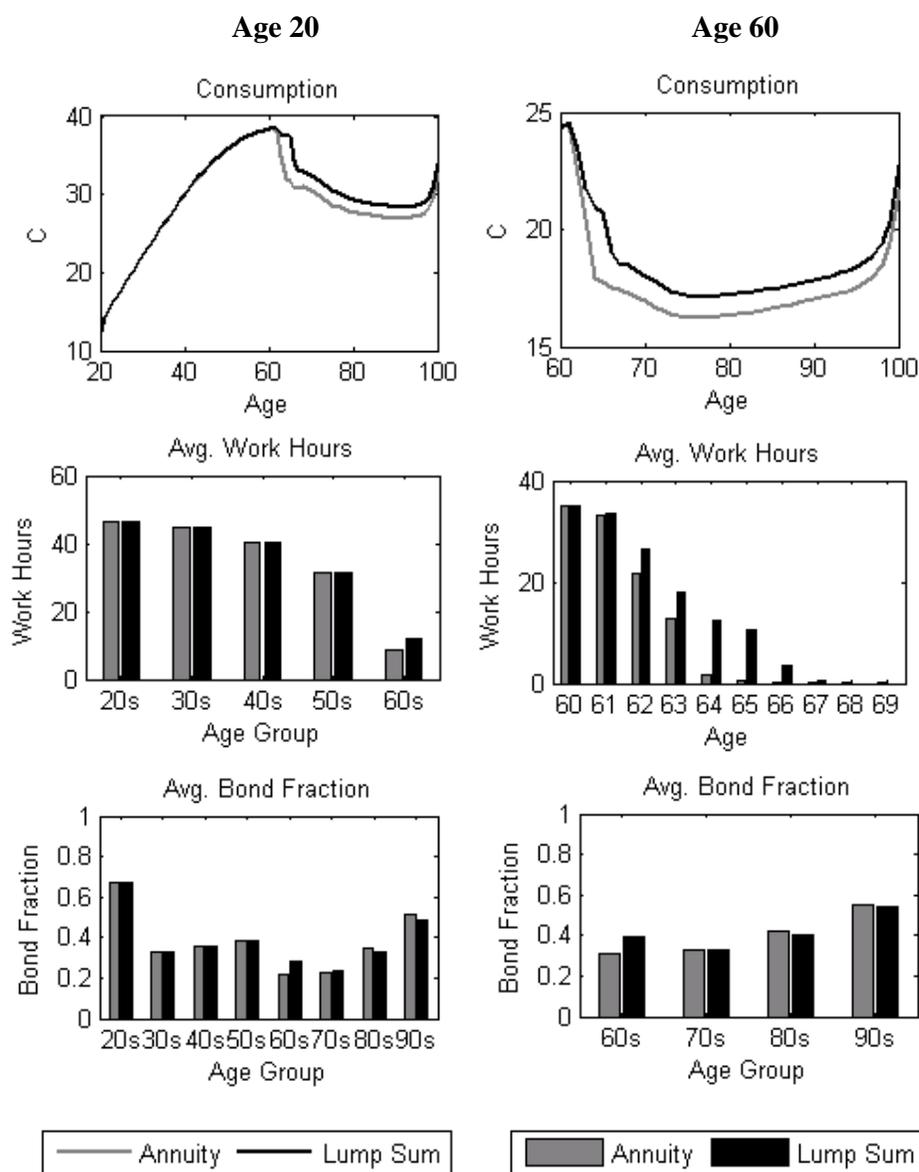
$$q_{it} = \text{constant} + B_1 * \text{age} + B_2 * \text{age}^2 + B_3 * \text{age}^3 + B_4 * \text{economy} + \varepsilon_{it}$$

Results of this regression analysis are summarized in the following table:

	Coefficient	t-Statistic	Standard Errors
Constant	0.5773585	49.51	0.011661
Age	-0.0132081	-17.57	0.000752
Age <sup>2</sup>	0.0001793	11.83	0.000015
Age <sup>3</sup>	-5.72E-07	-5.97	0.000000
Economy	0.0016453	1.61	0.001022
No. of Observations			161,050
R-Squared			0.021

Our results are compatible with observed rates of higher housing spending especially at older ages, unlike Gomes and Michaelides (2005) who assume that housing expenditures are zero over age 80.

**Figure 1: Impact of Lump Sum vs. Annuity Reward for Delayed Retirement on Consumption, Work Hours, and Investments among the Financially Sophisticated**



*Notes:* Expected life cycle profiles for financially sophisticated households with access to the stock market. Annuity: Delayed retirement benefits are paid as a lifelong increase of the pension annuity. Lump Sum: Delayed retirement benefits are paid as an actuarially fair one-time lump sum at retirement. Consumption at various ages reported in USD thousands. Work hours and bond fraction reported as average for different age groups. Base case calibration: relative risk aversion  $\rho = 5$ , bequest motive strength  $b = 0$ , time preference  $\beta = 0.97$ , leisure preference  $\alpha = 1.3$ , normal retirement age  $NRA = 65$ , early retirement age  $ERA = 62$ , latest retirement age  $LRA = 70$ , Social Security replacement rate  $\lambda = 0.6$ . Source: Authors' calculations.

**Table 1: Impact of Lump Sum vs. Annuity Reward for Delayed Retirement on Retirement Age: Base Case**

Age	Age 20		Age 60	
	Annuity	Lump Sum	Annuity	Lump Sum
62	1.7	1.0	14.7	8.1
63	30.8	5.6	36.9	22.1
64	26.9	4.1	37.2	17.2
65	11.7	3.0	7.0	3.5
66	19.3	46.9	3.7	29.1
67	7.1	20.0	0.4	14.8
68	2.3	19.4	0.1	5.2
69	0.1	0.0	0.0	0.0
70	0.1	0.0	0.0	0.0
Av. Ret. Age	64.5	66.3	63.5	64.9
P(RA>NRA)	28.9	86.3	4.2	49.1

*Notes:* Simulated distribution of retirement ages (frequency in %) for the base case. Assumed parameters: relative risk aversion  $\rho = 5$ , bequest motive strength  $b = 0$ , time preference  $\beta = 0.97$ , leisure preference  $\alpha = 1.3$ , normal retirement age  $NRA = 65$ , early retirement age  $ERA = 62$ , latest retirement age  $LRA = 70$ , Social Security replacement rate  $\lambda = 0.6$ ; financially sophisticated households with access to the stock market. Annuity: delayed retirement benefits are paid as a lifelong increase of the pension annuity. Lump Sum: delayed retirement benefits are paid as an actuarially fair one-time lump sum at retirement. P(RA>NRA): simulated frequency (in %) of retirement after the normal retirement age. Source: Authors' calculations.

**Table 2: Impact of Lump Sum vs. Annuity Reward for Delayed Retirement on Retirement Age: Alternative Calibrations**

	Age 20				Age 60			
	Annuity		Lump Sum		Annuity		Lump Sum	
	Av. Ret. Age	P(RA>NRA)						
<b>A. Financially Sophisticated</b>								
Base Case	64.5	0.289	66.3	0.863	63.5	0.042	64.9	0.491
<i>Alternative Household Preferences</i>								
$b = 2$	64.3	0.235	66.2	0.859	63.3	0.022	64.6	0.460
$b = 5$	64.3	0.240	66.2	0.844	63.3	0.023	64.4	0.409
$\beta = 0.96$	64.0	0.172	65.2	0.541	63.2	0.013	63.9	0.254
$\beta = 0.99$	65.4	0.536	66.4	0.887	64.0	0.136	65.7	0.738
$\rho = 2$	62.7	0.001	64.3	0.351	63.6	0.014	66.9	0.935
$\rho = 8$	63.0	0.028	62.9	0.002	62.5	0.000	62.5	0.000
$\alpha = 0.7$	68.8	0.955	68.3	0.934	68.1	0.993	68.3	0.995
$\alpha = 1.9$	62.6	0.007	62.7	0.016	62.5	0.000	62.5	0.002
<i>Alternative Retirement System Parameters</i>								
$\lambda = 0.45$	67.2	0.927	67.3	0.927	66.8	0.976	67.4	0.990
$NRA = 67$ (for age 20)	65.3	0.068	65.6	0.187	na	na	na	na
<b>B. Financially Unsophisticated</b>								
Base Case	67.0	0.898	66.7	0.963	63.9	0.092	64.0	0.186
$\rho = 2$	65.1	0.587	67.2	0.969	64.9	0.267	66.2	0.882
$\rho = 8$	64.2	0.257	63.7	0.091	62.7	0.001	62.7	0.000

*Notes:* Panel A (B) refers to simulated retirement patterns of households with (without) access to the stock market. P(RA>NRA): simulated frequency of retirement ages (RA) older than the normal retirement age (NRA). Annuity: delayed retirement credit paid as increase in Social Security lifetime benefit. Lump Sum: delayed retirement credit paid as an actuarially fair one-time lump sum at retirement. For base case parameters see Table 1. Source: Authors' calculations.

**Table 3: Welfare Implications of Lump Sum vs. Annuity Reward for Delayed Retirement**

	Age 20	Age 60
<b>A. Financially Sophisticated</b>		
Base Case	-0.001	0.041
<i>Alternative Household Preferences</i>		
$b = 2$	-0.001	0.043
$b = 5$	-0.001	0.042
$\beta = 0.96$	0.000	0.028
$\beta = 0.99$	-0.005	0.078
$\rho = 2$	0.000	0.289
$\rho = 8$	-0.006	0.000
$\alpha = 0.7$	-0.008	0.343
$\alpha = 1.9$	-0.001	0.000
<i>Alternative Retirement System Parameters</i>		
$\lambda = 0.45$	-0.005	0.223
$NRA = 67$	-0.001	na
<b>B. Financially Unsophisticated</b>		
Base Case	-0.020	0.008
$\rho = 2$	0.000	0.177
$\rho = 8$	-0.101	0.000

*Notes:* Welfare increases (in multiples of labor income as of age 20/60) from paying the delayed retirement credit as an actuarially fair one-time lump sum at retirement instead of an increase in the Social Security lifetime benefit. Base case calibration: relative risk aversion  $\rho = 5$ , bequest motive strength  $b = 0$ , time preference  $\beta = 0.97$ , leisure preference  $\alpha = 1.3$ , normal retirement age  $NRA = 65$ , early retirement age  $ERA = 62$ , latest retirement age  $LRA = 70$ , Social Security replacement rate  $\lambda = 0.6$ . Source: Authors' calculations.